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CYCLOTRON ECHO PHENOMENA

Roy W. Gould

Technical Report no. 28

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## CYCLOTRON ECHO PHENOMENA

Roy W. Gould

### Introduction

First I'd like to ~~restate~~ that not all the effects which I plan to discuss are really echo phenomena, so a slightly more appropriate title might be "Pulse Stimulated Cyclotron Radiation in Plasmas". However, all of the work was in fact motivated by the very interesting and important discovery of R. M. Hill and D. E. Kaplan at the Lockheed Laboratories earlier this year. Their work was published in the June 23 Physical Review Letters<sup>1</sup>, and a number of physicists immediately set out to try to understand the effect; the observation of echo radiation when a plasma is subjected to multiple pulses of radiation at the cyclotron frequency. At the November 1965 meeting of the Plasma Physics Division in San Francisco, this had already resulted in four papers: by Hill and Kaplan<sup>2</sup>, by J. Hirschfeld<sup>3</sup>, by W. H. Kegel<sup>4</sup> and by myself<sup>5</sup>. I'll try to summarize some of the important ideas which have been developed to date.

It was the fact that one could not directly carry over the nice ideas of Hahn<sup>6</sup> and Purcell<sup>7</sup> about spin echoes to cyclotron echoes that attracted people to work on this problem. Basically, although precessing spin system and gyrating charge particle systems have formal similarities, there are some essential differences which, I hope, will become more evident as this talk proceeds.

First, let me summarize in a very gross fashion, the experimental results (Refer to Figure 1). A short (10-20 nanosecond) pulse of radiation at the cyclotron frequency causes the plasma to develop a macroscopic current (or polarization) which decays after the removal of the pulse. A











at E, for example, and diagram (d) is in shape a circle, but elliptical. The curve in diagram (e) is therefore slightly distorted so that particles near A contribute slightly less current and the exact cancellation at time  $\tau$  is spoiled and an "echo" produced. Its amplitude is roughly  $\sqrt{1/c^2}$  times smaller than the instantaneous plasma response. The amplitude of subsequent echoes is proportional to higher powers of  $\sqrt{1/c^2}$ , and are very weak.

Another nonlinear mechanism which can spoil the exact cancellation and therefore lead to echoes is an energy-dependant cyclotron frequency, such as is caused by the relativistic mass effect. Particles along HAB have a higher rotational energy than those along DEF and would therefore have a slightly reduced rotation rate. They therefore appear rotated clockwise in (e) and (f) and therefore spoil the symmetry with respect to the  $V_x$  axis. This effect, although it is due to the relativistic shift in cyclotron frequency, is, in general, much more important than the first, since it is actually the relativistic change in phase which matters and this is approximately  $\sqrt{1/c^2}$  times the rotation angle in the laboratory system (typically  $10^4$ ).

Furthermore, Hirschfield pointed out in his San Francisco talk that there are other, possibly more important, reasons for the cyclotron frequency to be energy dependent. For example, in a non-uniform static magnetic field the cyclotron period depends on the orbit size and hence upon the rotational energy. As a very simple example, a rotationally symmetric magnetic field whose strength decreases with radius, leads to a cyclotron frequency which decreases with the particle energy. Spatially non-uniform static electric fields, which may also be present, also can give rise to an energy-dependent cyclotron frequency.

Still another possible mechanism suggested originally by James Van Allen of the Bell Telephone Laboratory and discussed quantitatively by Bill



and Kaplan at San Francisco, in the energy-dependent collision process. Although we have not yet considered the effect of an elastic collision is to alter the phase of a particle in a random way and effectively remove it from further consideration--at least in the two-pulse case. If, however, the removal process is energy dependent, more particles will be removed, for example, from HAB than from DMF (when the collision frequency increases with energy). Again the cancellation at times  $t = \pi\tau$  does not occur and echoes result.

Now I would like to digress a moment to discuss the spin echo effect from this point of view. Figure 5 shows the equation obeyed by an individual magnetic moment  $M$  in the absence of relaxation effects.  $\omega$  is proportional to the applied field  $H$ , which consists of superimposed static and r.f. fields,  $\omega_0$  and  $\omega_1$ , respectively. It follows from the first equation that the magnitude of  $M$  is a constant and therefore the tip of  $M$  vector lies on a sphere. In nuclear induction experiments one observes only the projection of the macroscopic magnetization, which is the sum of the individual moments, in the x-y plane. The last equation describes this perpendicular part of  $M$ , and it is similar in some respects to the previous equation for electron velocity. Note that free precession frequency is independent of  $M$  (i.e., "energy"-independent) but that the driving force is nonlinear, since it is proportional to  $M$  as well as to  $\omega_1$ .

The driving force nonlinearity can perhaps be seen more clearly in the diagram, where the circle centered on the origin represents a distribution of moments with different phases. (The vectors describe a cone--we see the projection of their tips on the x-y plane.) A r.f. pulse which

rotates each of the moments about the y axis through angles about  $30^\circ$  and  $60^\circ$  results in the ellipse-like projection. Obviously in this diagram different moments appear to experience different translations in the xy-plane, depending on the value of  $\theta$  which they had to begin with. While spin echoes employing pulses which rotate the moments through exactly  $90^\circ$  and  $180^\circ$  have very simple explanations, given by Hahn and Purcell, any combination of two non-infinitesimal pulses produces an echo.

Furthermore, any two-state quantum-mechanical system, spin or otherwise, can be cast into the same mold<sup>2</sup> as Figure 6 indicates. If the wave function can be described as a linear superposition of  $\psi_a$  and  $\psi_b$  then the amplitudes  $a$  and  $b$ , or rather certain quadratic combinations of them, obey a simple three-component vector equation which has the same form as the spin equation. Furthermore in the case of electric or magnetic dipole transitions  $\mu_1$ ,  $\mu_2$  and  $\mu_3$  are the expectation values of the dipole moment,  $\omega_3$  is the energy difference,  $\omega_1$  and  $\omega_2$  are combinations of the matrix elements of the driving perturbation between states a and b.

We may interpret this to mean that any ensemble of two-state quantum-mechanical systems which has a spread in transition frequencies with sufficient lifetimes could exhibit echoes.

Indeed, this is the proposed explanation of the photon-echo observed in ruby by the Columbia group: Kurait, Abella and Hartmann<sup>3</sup>. The levels involved are electronic states in chromium which are split by the crystal electric field.

I would now like to outline the mathematical treatment that goes with these diagrams (refer to Fig. 7).  $V'$  is the complex velocity of a particular electron whose difference cyclotron frequency is  $\omega'$  at a time  $t$  measured from the

second pulse. The first pulse produces velocity  $V_1$  and between the two pulses the velocity vector is rotated through an angle  $\phi_1$  -- remember the coordinate system is rotating to the rotating electric field and  $\omega_c'$  is the cyclotron rotation frequency relative in the rotating system. The second pulse provides an additional velocity  $V_2$  and the total velocity vector rotates through an angle  $\phi$  in the next interval.

To obtain the macroscopic plasma current  $\tilde{J}$  we need to multiply both by the number of particles which have a difference cyclotron frequency  $\omega_c'$  and by the probability that these particles survive until time  $t$  without making a phase-destroying collision, and then integrate over  $\omega_c'$ .

For the three types of nonlinearities already discussed, either  $V_2$ ,  $\phi$  or  $P(t)$  are energy dependent, according to whether the driving force, the cyclotron frequency, or the collision frequency is energy dependant.

Figure 8 outlines a simplified treatment of what are probably the two most important nonlinearities in plasmas. I have assumed, for simplicity, that both the cyclotron and collision frequencies have a weak dependence on  $v^2$ , i.e., upon energy. This is a good approximation for the cyclotron frequency and not so good for the collision frequency, but it serves to illustrate the point. Mill and Kaplan<sup>2</sup> have given results for other more realistic dependences of collision frequency on velocity.

Between the two pulses all particles have the same energy,  $V_1^2$ ; collision effects are unimportant. After the second pulse, however,  $V^2$  depends on  $V_1$ ,  $V_2$  and  $\phi_1$ , the phase the particle had at the time of the second pulse. Since both  $\phi$  and  $v$  appear in the exponent, the  $\phi_1$  will appear in the

exponent and we also used the half-angle Bessel function identity -  
Note particularly the  $\frac{\partial \omega}{\partial v}$  in which the two effects appear,  
so that we can compare their relative importance by comparing  $\frac{\partial \omega}{\partial v}$  directly with  $\frac{\partial \omega}{\partial v^2}$ . Now  $\omega_c$  is very large compared with  $v$ , but the relative dependence on  $v^2$  is much weaker. It is therefore not clear, a priori, which effect is more important.

After a few minor steps one obtains an expression for the plasma current which has the form of a series of pulses. Centered on  
The pulse shape is given by the Fourier transform of the cyclotron frequency distribution function. A very inhomogeneous field leads to narrow echo pulses. The amplitude factors contain the Bessel functions and are slowly varying functions of time.

Figure 9 shows the manner in which the amplitude of the first echo pulse depends upon time in these two theories. Note that they all have the same general appearance, rising at first as either nonlinear effect allows the echo to develop, and finally falling as collisions take their toll. The dashed and solid curves are for energy-dependent collisions and cyclotron frequencies, respectively. As the magnitude of energy dependence becomes larger, so does the maximum achievable echo pulse amplitude. A pure exponential decay line is shown for comparison and one sees that even for large times is only approximately exponential. If the two pulses have unequal strengths, the decay curve for energy dependent cyclotron frequencies develops periodic local minima and this may be a way to differentiate between the two effects.

Another important effect may also contribute to decay of the echo pulses: As a result of their relatively small thermal velocities, a certain

can move along a magnetic field line and change its cyclotron frequency slightly. The resonance change in phase, since it is different for the particles with different speeds, will lead to a decay

$$- \frac{1}{4} \left( \frac{\partial \omega}{\partial z} \frac{c}{v_{th}} t^2 \right)^2$$

which becomes a very strong effect after a certain time.

Now I'd like to turn to the three-pulse case to see why it is possible, despite many many collisions between the second and third pulses, for the system to still remember the time interval between the first two pulses,  $\tau$ . The central idea here is that these are essentially elastic collisions, since the electrons collide with heavy particles. Figure 10 shows the effect of the three-pulse sequence on an ensemble of particles. The first pulse imparts the same velocity to all (first diagram) and they disperse because of the different cyclotron frequencies (second diagram). The second pulse translates the circle (third diagram). During the long time interval between the second and third pulses, each particle experiences many collisions, distributing particles with the same speed over a spherical shell. Prior to the third pulse, particles with different energies are distributed over different spherical shells ABC... according to their energy, i.e., according to the phase they had at the time of the second pulse. The third pulse translates each spherical shell, and they disperse as before. Thus we have particles distributed in shells, onion-like in character, with particles in the same shell having experienced the same phase change, modulo  $2\pi$ , between the first and second pulse. During the next interval  $\tau$ , the particles on a given shell turn through the same angle as they did in the first interval  $\tau$  and we

achieve the situation in the lower part. The center of the spheres has its center on the lower sphere and the vector would again exactly cancel were it not for nonlinear effects. Energy-dependent collisions will selectively remove particles from various regions of shell A and thereby change its center of charge. An energy-dependent cyclotron frequency will shift its center clockwise, etc. In either case no cancellation is spoiled and an echo response results. The last figure shows the situation at the time of the second echo, which also arises from nonlinear effects. One yet very puzzling feature is the long decay time observed in the three-pulse case.

When the electron density is higher, earlier in the decay, the echo effect appears to occur at the upper hybrid frequency<sup>2</sup>.  $\omega^2 = \omega_p^2 + \omega_c^2$  and collective effects are probably important. A major extension of these ideas will be required.

So much for the phenomena ordinarily regarded as echoes. In trying to understand Hill and Kaplan's experiment, several false starts were made which actually led to new predictions. First there is the single pulse case of J. Hirschfield<sup>3</sup>. He observed, as Figure 11 illustrates, that in a very homogeneous field a single applied pulse might produce a train of responses. Consider plasma electrons which all have the same speed perpendicular to the magnetic field  $B$  with random phases, and no velocity along  $B$ . A single, very weak pulse translates each velocity vector an amount small compared with  $v_D$ . Some particles have their energy very slightly increased, some very slightly decreased, and some not at all. If the gyro frequency is energy dependent there is a differential rotation, shown by the arrows, which causes the particles to bunch at  $\theta = -\pi/2$ , disperse and bunch at  $\theta = \pi/2$ .

etc. The expression for the resulting current is given on the slide and  $J^2$  is plotted. It is especially that nearly the full plasma current  $Ne v_0$  is eventually achieved, but one must wait longer, the smaller the stimulating pulse is. After integrating over a Maxwell distribution of perpendicular velocities, the effect survives, although reduced in amplitude and with but a single maximum in current.

Probably the mono-energetic initial state first considered by Hirschfield could be produced by the application of a pulse itself. However, the interval between the responses produced by the second applied pulse would depend on the amplitude of the second applied pulse, not the time interval between the two applied pulses. Wilhelm Kegel, also trying to understand the echo experiment, found yet another effect. Suppose that the magnetic field is very uniform, the cyclotron frequency is energy dependent, and the electrons have a thermal distribution of velocities. After the first pulse (refer to Figure 12), the particles disperse because of the energy-dependent cyclotron frequency, together with the thermal energy spread. A second pulse produces the thick ring shown in (c). The interesting result is that following the decay of the instantaneous response to the second applied pulse a series of responses results. I haven't been able to see how to explain this clearly with diagrams yet.

Figure 13, from Kegel's work<sup>4</sup> shows that these responses are not separated by the interval  $\tau$  but by  $\tau/2$ . In this computation the two pulses have equal strength. For two unequal pulses, the responses are separated by an interval

$$\tau \left( \frac{v_2}{v_1} + 1 \right)$$

and there is a second, weaker train whose interval is



$$\left| \frac{A^2}{v_1} - 1 \right|$$

Kegel has also shown that when the energy dependent cyclotron frequency is involved, a sufficiently strong inhomogeneity in the magnetic field will destroy his effect. Similarly, he has shown that sufficiently high thermal speeds (temperature) will destroy the ordinary echo in a non-uniform magnetic field.

He has also shown that for three pulses, without collisions, a multiplicity of responses occur at times

$$t = n_1 + m_2 + n_3, \quad \text{all integral } m, n \text{ for which } t > 0$$

(t measured from third pulse)

Finally, I would like to discuss echo phenomena in a more general context. We saw that two level quantum mechanical systems obeyed equations similar to "classical" spin equation. so by analogy, echoes could be obtained in ensembles of such systems. It is characteristic of two-level systems that an applied perturbation which resonates with the natural frequency of the system alternately increases and decreases its energy and the nonlinearity required for the echo is immediately evident.

Such is not the case for an ensemble of classical (or quantum) harmonic oscillators such as gyrating charged particles, for there the energy is increased indefinitely (or until more subtle nonlinear effects enter) by a resonant driving force. This is a basically different type of system.

Now our treatment of echo phenomena is, at best, qualitatively at least and quantitatively perhaps, to oscillator systems.

general. Figure 1b illustrates my point. I employ coordinates  $q$  and  $p$ , the momentum and frequency axes coordinates, respectively. To the  $p, q$  phase plane, circles are circles and by introducing a rotating coordinate system  $q', p'$  which rotates with frequency of the driving force, the rotating component is constant and the other has a negligible effect. Observable quantities might be  $\langle p \rangle$  or  $\langle q \rangle$  for example. In short, all our previous ideas can be carried over to a general oscillator system.

Basically we require for echo phenomena in a system:

- a) An ensemble of oscillators with a narrow distribution of natural frequencies, which interact with external forces
- b) Sufficiently long relaxation times to permit observation
- c) One of a variety of nonlinear effects to "spoil cancellation"
  1. energy-dependent driving force
  2. energy-dependent natural frequency--anharmonic oscillator
  3. energy-dependent relaxation phenomena
  4. others?

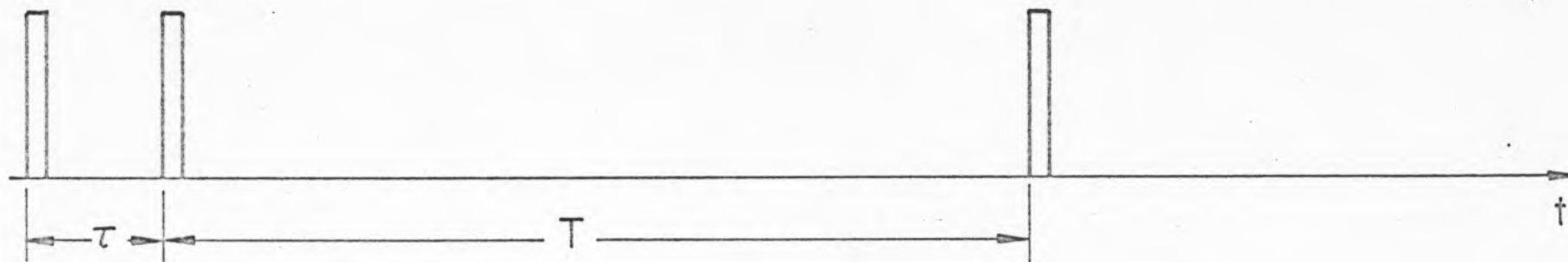
It is interesting to note that these conditions are essentially the same as required for use in masers and lasers.

You can see that Hill and Kaplan's discovery has indeed stimulated a considerable interest, some new and potentially useful results, particularly in measuring collision rates at low energies  $< 1$  electron volt. Where it will lead remains to be seen, but it will provide many new problems to consider and, I think, ultimately a variety of new experimental techniques.

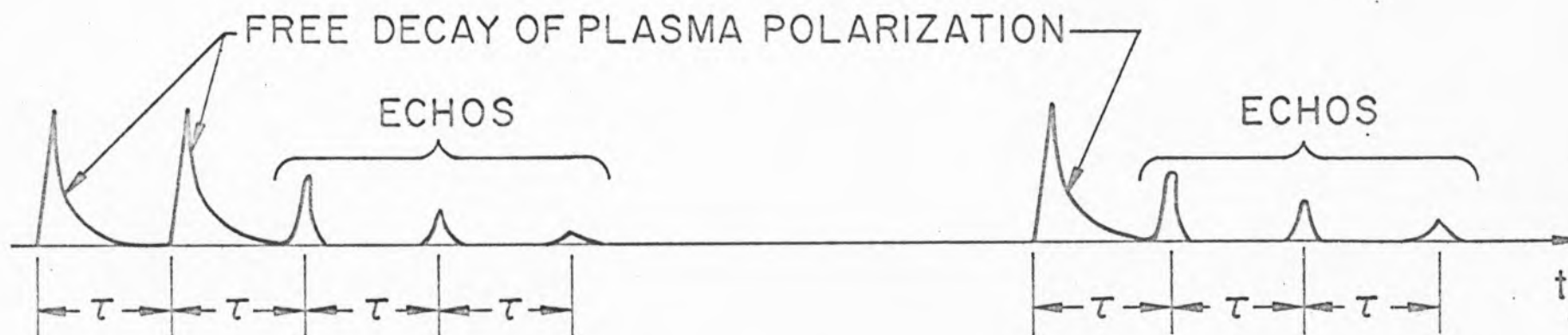
In closing I would like to acknowledge very fruitful discussions with W. H. Kegel, R. M. Hill, D. E. Kaplan and J. L. Hirschfield.

REFERENCES

1. R. M. Hill and D. E. Kaplan, Phys. Rev. Letters 14, 1062 (1965)
2. R. M. Hill and D. E. Kaplan, Bull. Am. Phys. Soc. (to appear)
3. J. L. Hirschfield and J. M. Wachtel, Bull. Am. Phys. Soc. (to appear)
4. W. H. Kegel, Bull. Am. Phys. Soc. (to appear); see also Physics Letters Dec. 15, 1965 issue, and Phys. Review (to appear).
5. R. W. Gould, Bull. Am. Phys. Soc. (to appear); see also Physics Letters Dec. 1, 1965 issue.
6. E. L. Hahn, Phys. Review 80, 580 (1950)
7. H. Y. Carr and E. M. Purcell, Phys. Review 94, 630 (1954)
8. R. P. Feynman, F. L. Vernon, and R. L. Hellwarth, Jour. Appl. Phys. 28, 49 (1957).
9. N. A. Kurnit, I. D. Abelle and S. R. Hartmann, Phys. Rev. Letters 13, 367 (1964).

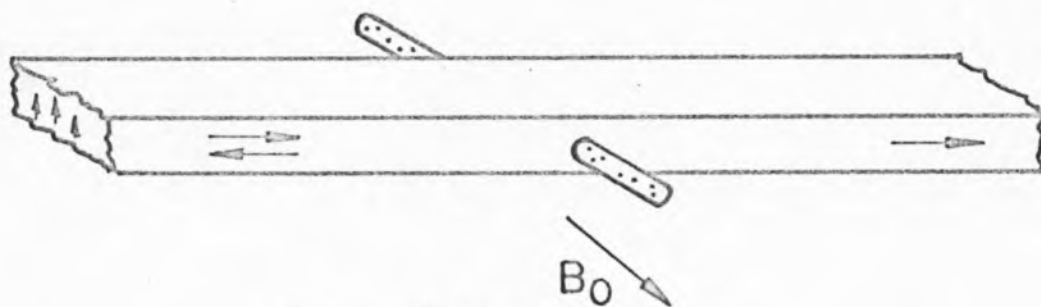
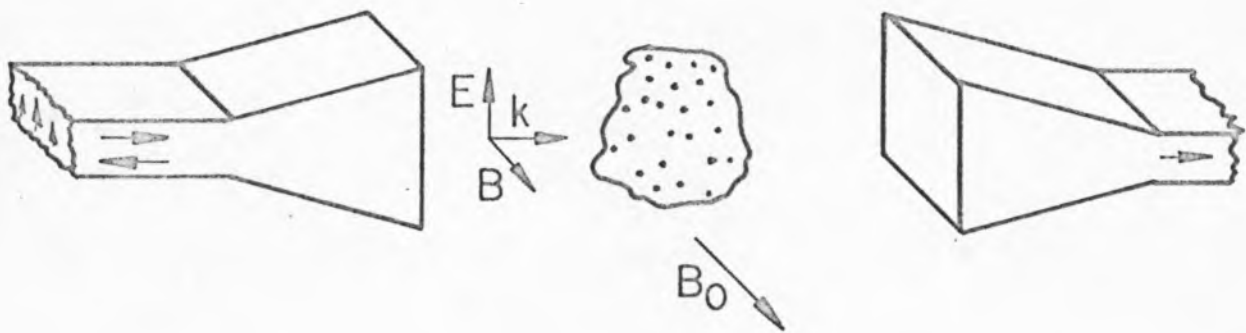


MAGNITUDE OF APPLIED RADIO FREQUENCY ( $\omega \approx \frac{eB_0}{m}$ ) FIELD

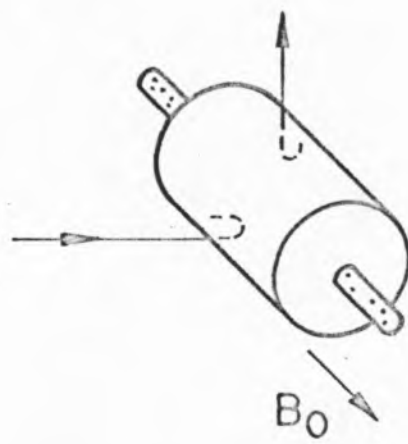


MAGNITUDE OF PLASMA RESPONSE

FIG. 1



$TE_{10}$  WAVEGUIDE



$TE_{III}$  CAVITY RESONATOR

FIG. 2

LINEARIZED EQUATION OF MOTION OF SINGLE ELECTRON:

$$\dot{\underline{V}} - \underline{\omega}_c \times \underline{V} = \frac{-e}{m} \underline{E} \qquad \underline{\omega}_c = \frac{e \underline{B}_0}{m}$$

AFTER TRANSFORMATION TO ROTATING VELOCITY SPACE:

$$\dot{\underline{V}}' - \underline{\omega}'_c \times \underline{V}' = \frac{-e}{m} \underline{E}' \qquad \underline{\omega}'_c = \underline{\omega}_c - \underline{\omega}$$

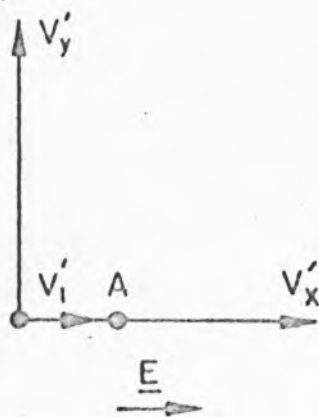
COMPLEX REPRESENTATION:  $\underline{V}' = V'_x + i V'_y$  ETC.

$$\dot{\underline{V}}' - i \omega'_c \underline{V}' = \frac{-e}{m} \underline{E}'$$

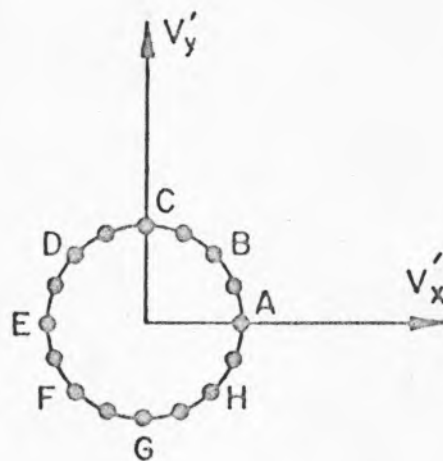
SOLUTION:

$$\begin{aligned} \underline{V}'(t) &= \underline{V}'(0) e^{i \omega'_c t} + \int_0^t e^{i \omega'_c (t-s)} \frac{-e}{m} \underline{E}'(s) ds \\ &\cong \underline{V}'(0) + \frac{-e}{m} \underline{E}' t \end{aligned} \qquad \begin{aligned} \omega'_c t &\ll 1 \\ \underline{E}' &\text{ CONSTANT} \end{aligned}$$

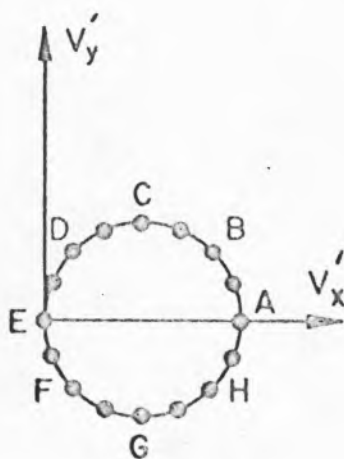
Fig. 3



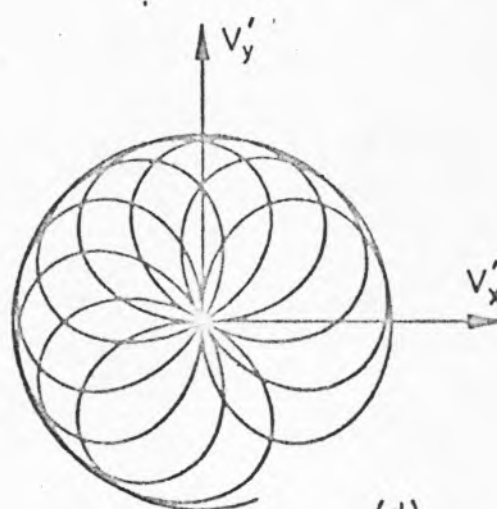
(a)



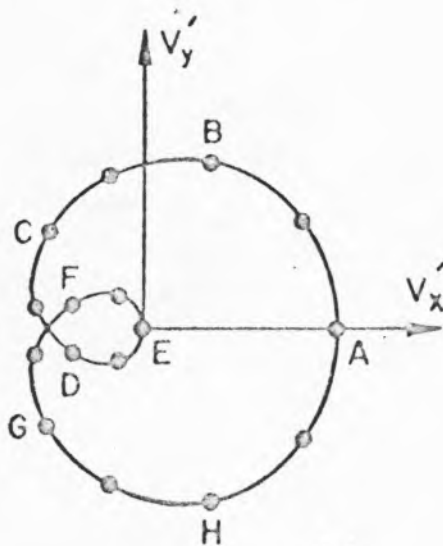
(b)



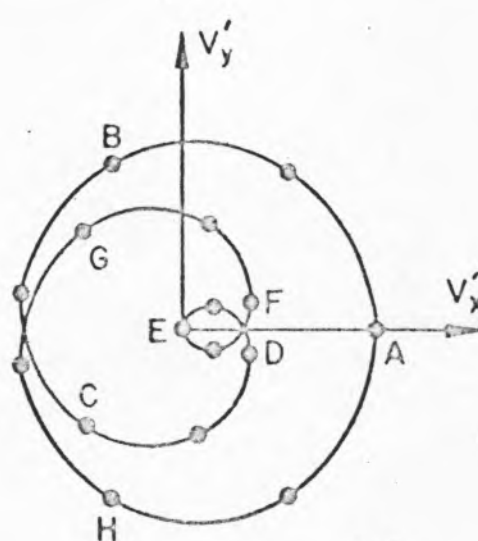
(c)



(d)



(e)



(f)

FIG. 4



### SPIN ECHO EQUATIONS:

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \underline{\omega} \implies |\mathbf{M}| = \text{CONSTANT}$$

$$\underline{\omega} = \gamma \mathbf{H} = \underline{\omega}_0 + \underline{\omega}_1$$

$$\underbrace{\frac{d\mathbf{M}_\perp}{dt} + \underline{\omega}_0 \times \mathbf{M}_\perp}_{\text{FREE PRECESSION}} = \underbrace{\mathbf{M} \times \underline{\omega}_1}_{\text{NON-LINEAR}}$$

$\omega_0$  = FREQUENCY      DRIVING FORCE

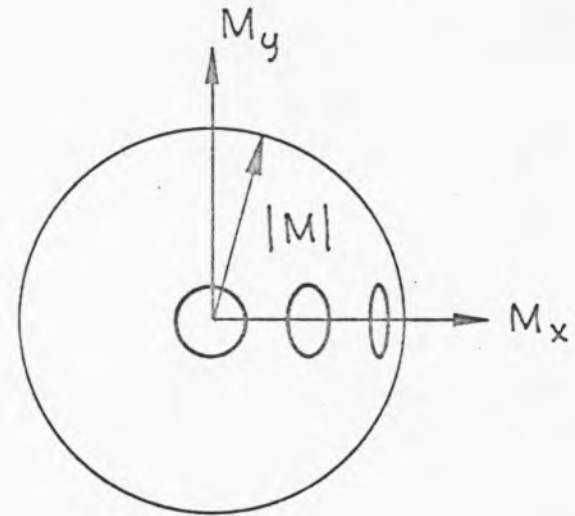


FIG. 5

## TWO STATE QUANTUM MECHANICAL SYSTEM

[FEYNMAN, VERNON, HELLWARTH JAP 28 49 (1957)]

$$\psi(t) = a(t) \psi_a + b(t) \psi_b$$

$$\frac{d\underline{r}}{dt} = \underline{\omega} \times \underline{r}$$

$$r_1 = ab^* + a^*b$$

$$\omega_1 = (V_{ab} + V_{ba})/\hbar$$

$$r_2 = i(ab^* - a^*b)$$

$$\omega_2 = i(V_{ab} - V_{ba})/\hbar$$

$$r_3 = aa^* - bb^*$$

$$\omega_3 = (E_a - E_b)/\hbar$$

Fig. 6

$$\vec{V}'(t) = (V_1 e^{i\phi_1} + V_2) e^{i\phi}$$

$$\vec{J}'(t) = -Ne \int d\omega'_c G(\omega'_c) \vec{V}'(t) P(t)$$

$$V_1 = \text{VELOCITY IMPARTED BY 1}^{\text{ST}} \text{ PULSE} \cong \frac{e}{m} E_1 t_1$$

$$V_2 = \text{VELOCITY IMPARTED BY 2}^{\text{ND}} \text{ PULSE} \cong \frac{e}{m} E_2 t_2$$

$$\phi_1 = \text{ROTATION BETWEEN 1}^{\text{ST}} \text{ AND 2}^{\text{ND}} \text{ PULSES} \cong \omega'_c \tau$$

$$\phi = \text{ROTATION AFTER 2}^{\text{ND}} \text{ PULSE} \cong \omega'_c t$$

$$P(t) = \text{PROBABILITY OF } \underline{\text{NO COLLISION}} \cong e^{-\nu(t+\tau)}$$

BETWEEN 1<sup>ST</sup> PULSE AND t

$$G(\omega'_c) d\omega'_c = \text{FRACTION OF ELECTRONS WITH}$$

DIFFERENCE GYROFREQUENCIES BETWEEN

$$\omega'_c \text{ AND } \omega'_c + d\omega'_c$$

FIG. 7

ENERGY DEPENDENT CYCLOTRON AND  
COLLISION FREQUENCIES :

$$J = -Ne \int G(\omega'_c) d\omega'_c [V_1 e^{i\phi_1} \pm V_2] e^{i\phi} e^{-\nu t}$$

$$\phi = [\omega_c(V^2) - \omega] t \cong [\omega'_c + \frac{\partial \omega_c}{\partial V^2} V^2] t$$

$$\nu t \cong [\nu_0 + \frac{\partial \nu}{\partial V^2} V^2] t \quad (\text{WEAK DEPENDENCE})$$

$$V^2 = V_1^2 + V_2^2 + 2V_1 V_2 \cos \phi_1 \quad \phi_1 = \omega'_c \tau$$

$$\text{NOW } e^{-(\alpha + i\beta) \cos \phi_1} = \sum_{-\infty}^{\infty} I_n(\alpha + i\beta) e^{-in\phi_1}$$

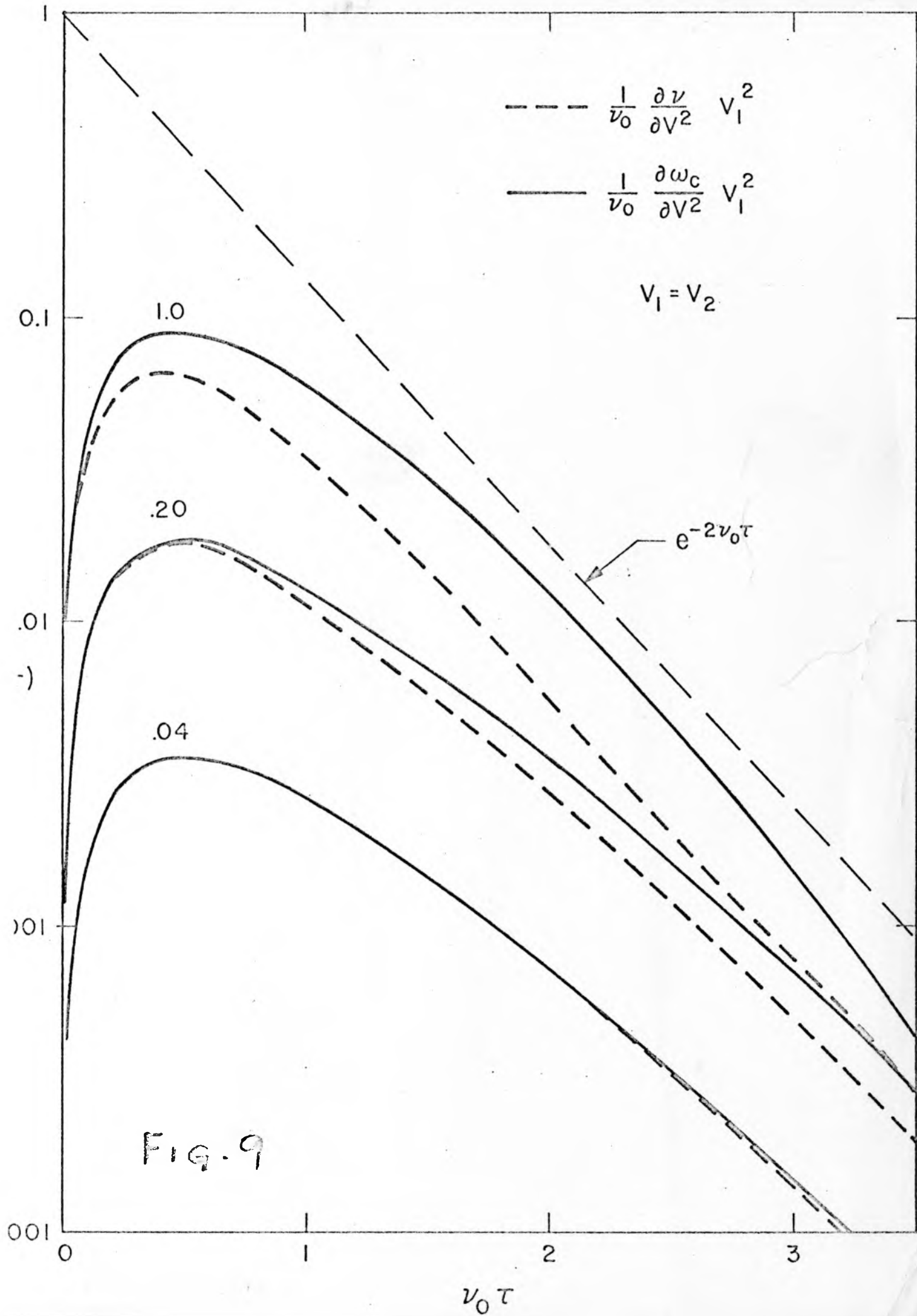
$$\text{WITH } \alpha = \frac{\partial \nu}{\partial V^2} 2V_1 V_2 t \quad \beta = \frac{\partial \omega_c}{\partial V^2} 2V_1 V_2 t$$

$$|J| = Ne V_1 \sum_{-\infty}^{\infty} A_n(t) g(t - n\tau)$$

$$g(t) = \int_{-\infty}^{\infty} G(\omega'_c) e^{i\omega'_c t} d\omega'_c \quad (\text{PULSE SHAPE})$$

$$A_n(t) = \text{PULSE } \underline{\text{AMPLITUDE}} \text{ FACTOR}$$

Fig 8



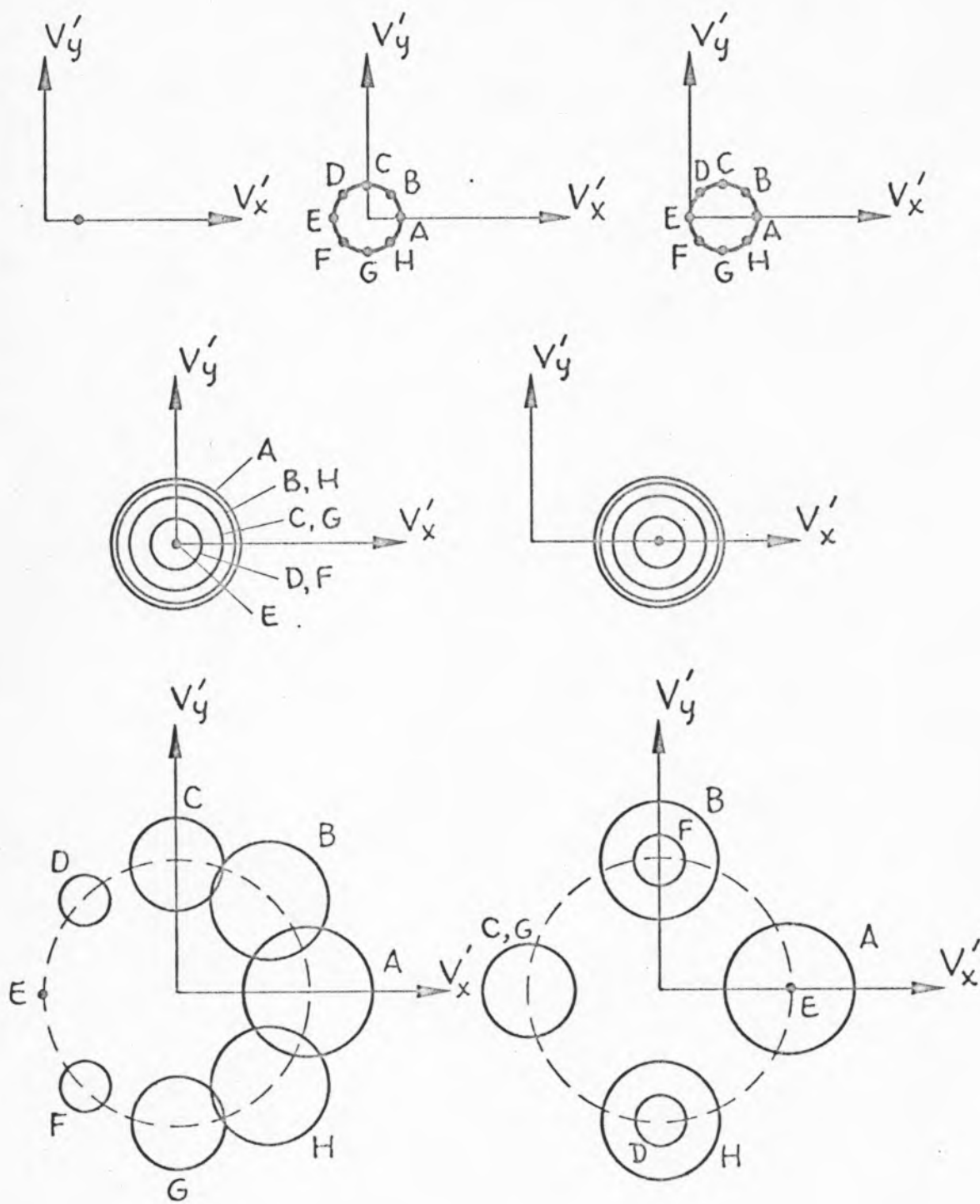
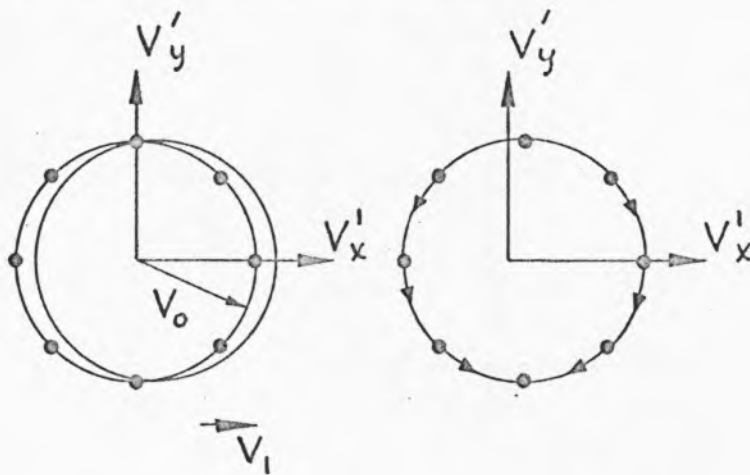


Fig. 10

# RESPONSE TO A SINGLE PULSE :



$$\phi \cong \phi_0 - \left( \frac{\partial \omega_c}{\partial V^2} \right) (V_0^2 + V_1^2 + 2V_1 V_0 \cos \phi_0) t$$

$$J'_y \cong -Ne V_0 J_1 \left( \frac{\partial \omega_c}{\partial V^2} 2V_1 V_0 t \right) \quad V_1 \ll V_0$$

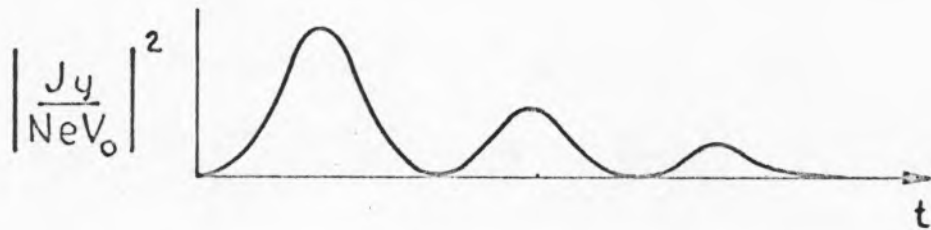


Fig. 11



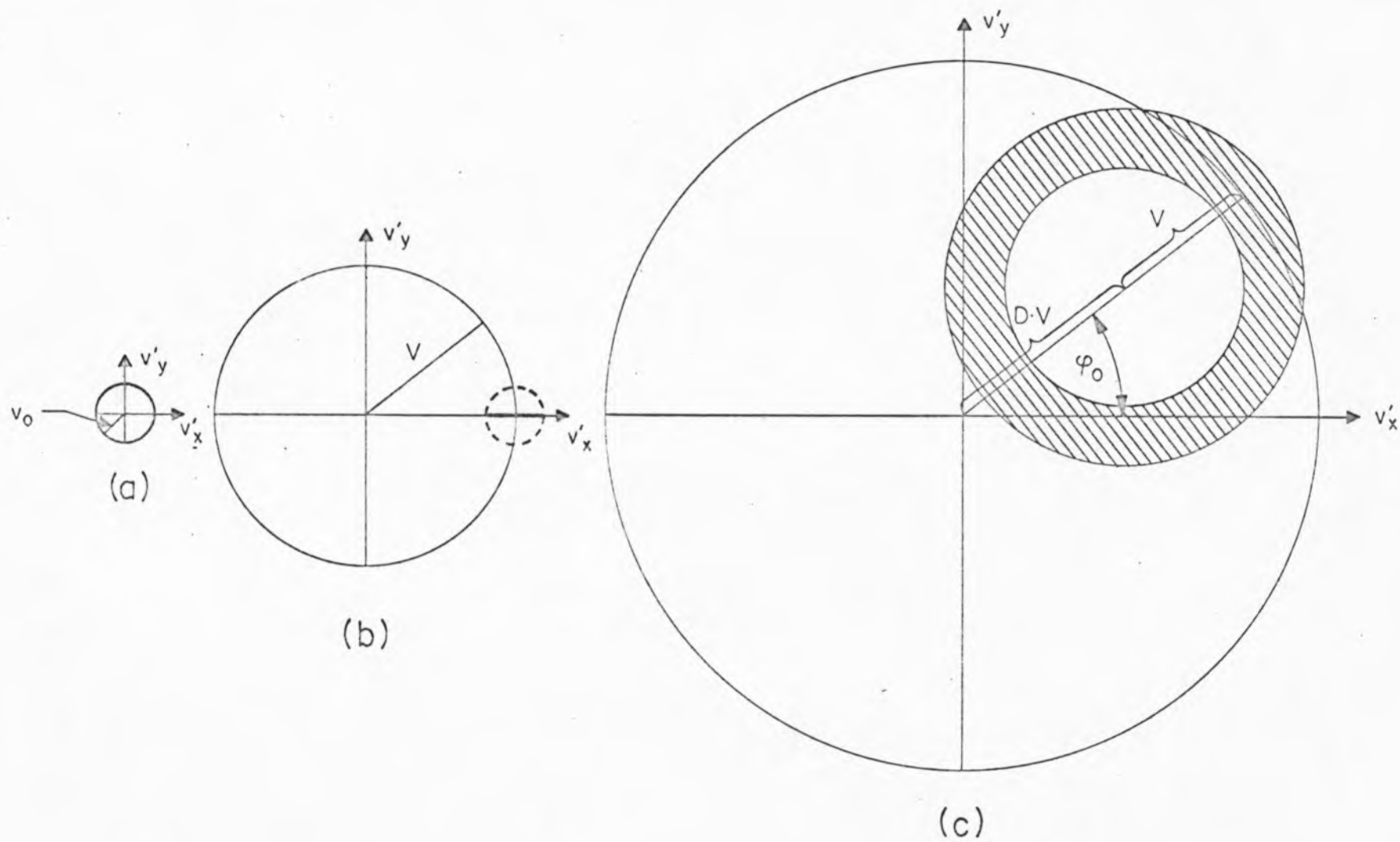
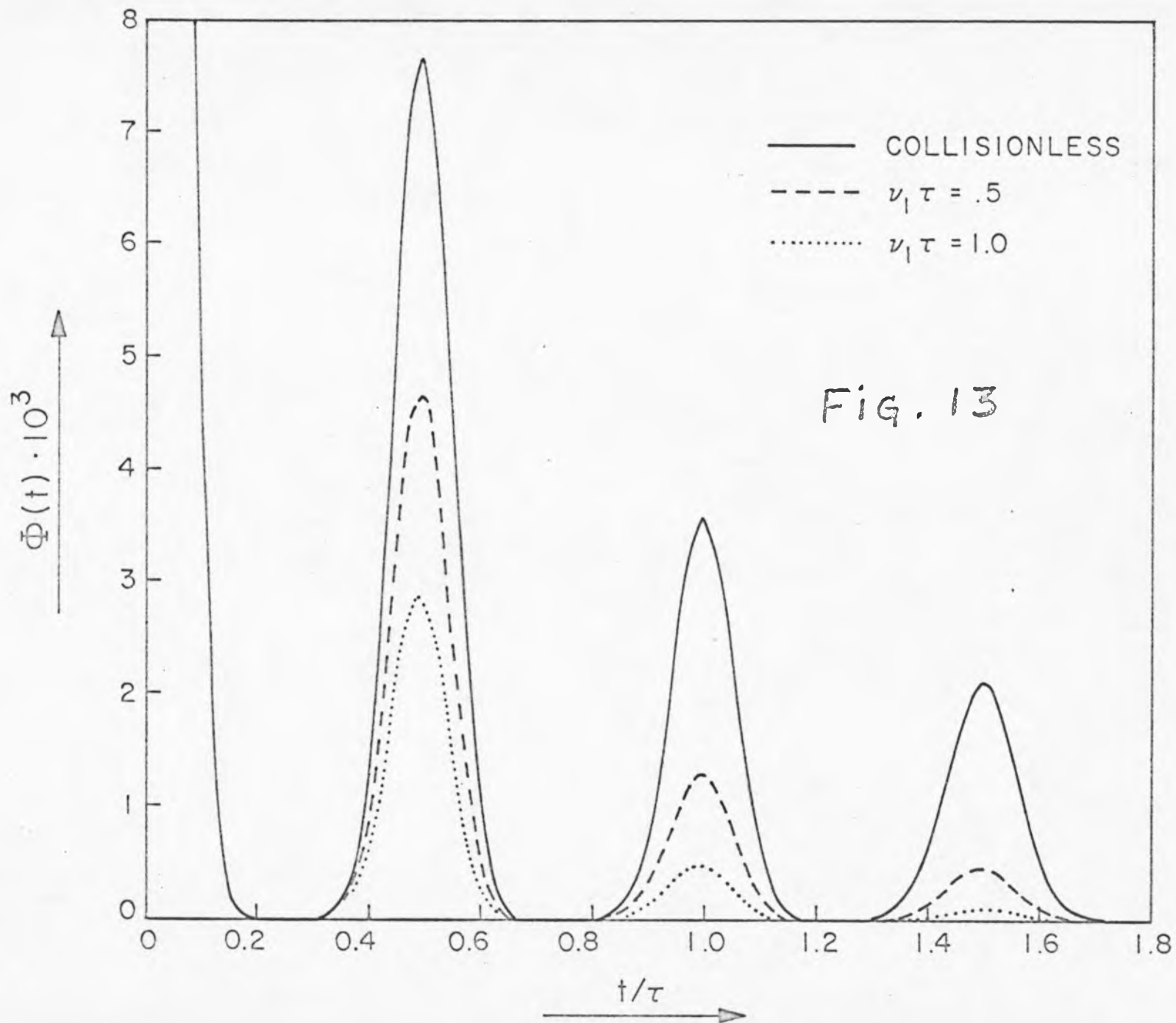
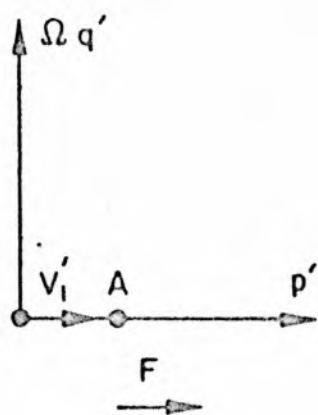
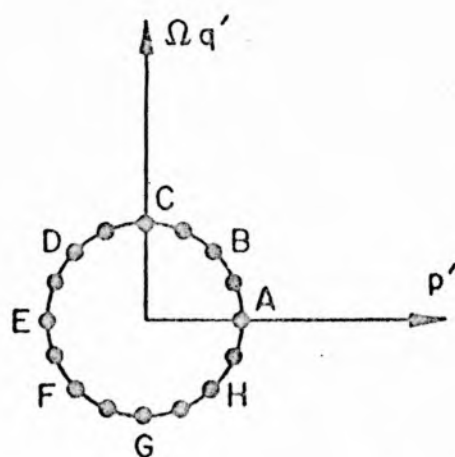


FIG. 12

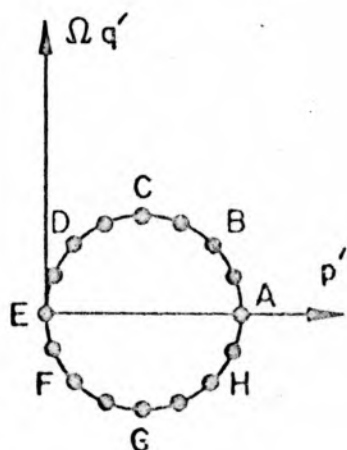




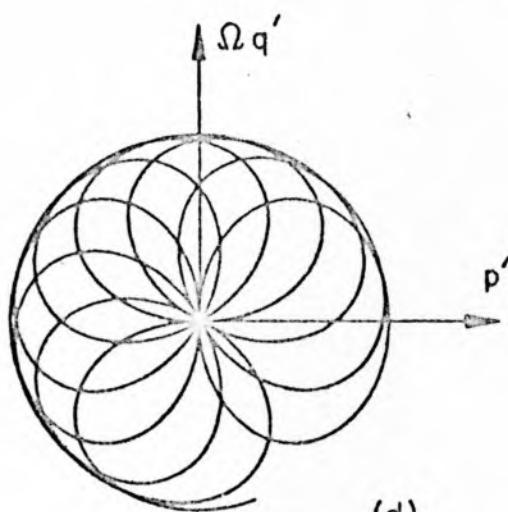
(a)



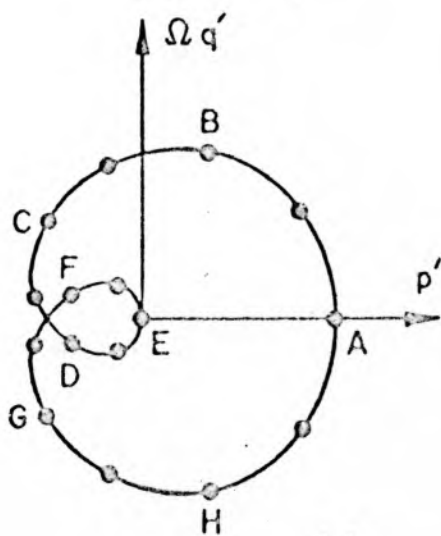
(b)



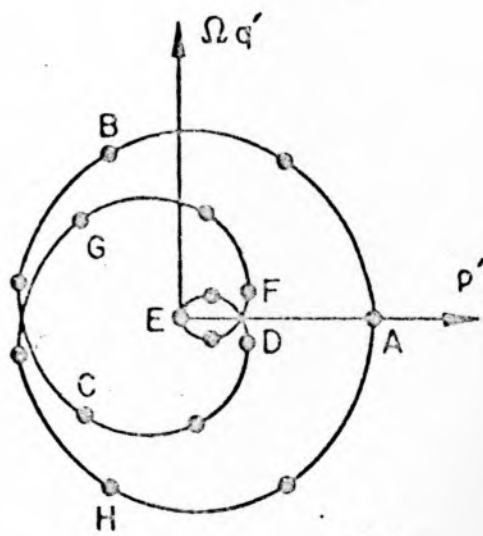
(c)



(d)



(e)



(f)

Fig. 14